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## SLOPPGEN: A Problem Generator for the Two-Dimensional Rectangular Single Large Object Placement Problem With Defects

Vera Neidlein/André Scholz/Gerhard Wäscher

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Single Large Object Placement Problem  
With Defects**

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**Abstract:** In this paper, a problem generator for the Two-Dimensional Rectangular Single Large Object Placement Problem is presented in which the large object includes one or several defective areas. The parameters defining this problem are identified and described. The features of the problem generator are pointed out, and it is shown how the program can be used for the generation of reproducible random problem instances.

**Keywords:** two-dimensional cutting, defect, problem generator

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## 1 Introduction

Two-dimensional cutting problems have been in the focus of researchers for many years. Since its beginnings (cf. Brooks et al. (1940), Gilmore and Gomory (1965)), different types of this problem have been widely studied in the literature. Starting in the 1960s, work has also been done on problems including material defects (e.g. Hahn (1968), Carnieri et al. (1993)), which are particularly relevant in practice.

There are still numerous publications in the field of two-dimensional cutting at the present time. Many of them deal with the challenge of developing exact algorithms that are faster than existing ones, or with developing faster and better-performing heuristics. The latter is due to the fact that most problems in the field of two-dimensional cutting are known to be NP-hard.

It is often difficult to draw general conclusions on the performance of an algorithm, because authors – in particular when dealing with real-world, “practical” problems – often only give the results for a few instances to demonstrate how their algorithm works. These instances usually either come from the practical problem considered, or they are taken from the literature (e.g. the OR library by Beasley (1990), problems presented by Herz (1972), Beasley (1985)) and treated as benchmark problems, although – sometimes having been used for decades – it is not known whether they still can be seen as valid benchmark problems. Both approaches make it almost impossible to carry over the results to problems with a different data structure. Having been not necessary for the first algorithms (as from Gilmore and Gomory (1965)), such systematical tests gain more importance with every new publication in this field due to the huge and still growing number of algorithms for two-dimensional cutting problems.

In order to overcome this lack of appropriate systematic test problem instances and provide general access to an un-biased basis of problem data for an important class of two-dimensional cutting problems, namely the so-called Rectangular Single Large Object Placement Problem (cf. Wäscher et al. (2007)), a problem generator has been developed that will be described in this publication. It can be used to easily generate a large number of problem instances with specific desired properties, and can thus enable researchers to follow a more systematic approach for testing algorithms with regard to the performance compared to existing algorithms and with regard to instances from problem classes of different data structures.

This paper is organized as follows: In Section 2, we introduce the Two-Dimensional Rectangular Single Large Object Placement Problem With Defects, for which this problem generator was designed. In Section 3, the parameters of the problem are identified and explained, which can be used to define classes of problems. Hence, homogeneous instances of a specific problem class can be generated randomly with the problem generator described in detail in Section 4. In Section 5, examples for instances from a specific problem class are given.

## 2 The Two-Dimensional Single Large Object Placement Problem

### 2.1 Standard Problem

The Two-Dimensional Rectangular Single Large Object Placement Problem (2D\_R\_SLOPP) is a standard Cutting & Packing problem which can be described as follows (cf. Wäscher et al. (2007)):

A large rectangle (large object) of given length  $L$  and width  $W$  is to be cut down in order to provide smaller rectangles (small items) of particular dimensions (types), i.e. of length  $l_i$ , width  $w_i$  and value  $v_i$  ( $i = 1, \dots, n$ ). It is imposed that all cuts lie parallel to one of the edges of the large object (orthogonal layout). The objective is to maximize the total value of the provided small items (output maximization problem). In our special case, the value of the item types corresponds to their area, i.e.  $v_i = l_i \cdot w_i$  (unweighted problem).

As a first-level standard problem (see Wäscher et al. (2007)), the 2D\_R\_SLOPP is characterized by the absence of additional constraints, i.e. there are no upper or lower bounds on the number of times an item type has to be cut from the large object (unconstrained problem), the items may have any orientation (vertical or horizontal) on the large object (no rotational constraint), the type of cutting is not restricted (non-guillotineable-constrained layout), and there are no upper or lower bounds on the number of cutting stages (non-staged problem).

Any layout of an assortment of small items on the large object such that the items do not overlap and lie entirely within the large object is called a feasible cutting pattern.

The 2D\_R\_SLOPP can now be formulated as a mathematical model:

$$\begin{aligned} \max \quad & \sum_{i=1}^n v_i \cdot z_i \\ \text{s.t.} \quad & (z_1, \dots, z_n) \text{ corresponds to a feasible cutting pattern.} \end{aligned}$$

Herein,  $(z_1, \dots, z_n)$  is said to correspond to a feasible cutting pattern if item type  $i$  ( $i = 1, \dots, n$ ) can be laid out  $z_i$  times on the large object in a way that a feasible cutting pattern is obtained.

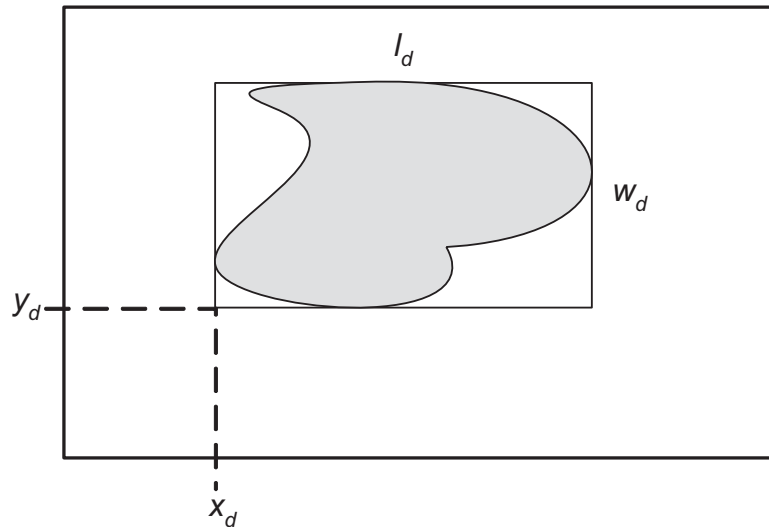
All the problem data introduced above can be assumed to be integer numbers without loss of generality since – as similarly described in Gau and Wäscher (1995) for a one-dimensional problem – the data  $L, W, l_1, \dots, l_n, w_1, \dots, w_n$  is only implicitly represented in the model formulation as it defines the feasible cutting patterns. Therefore, multiplying all the data with a constant factor  $m > 0$  results in an identical model formulation.

### 2.2 Problem Variant: Defects

The standard problem can be extended by introducing  $m$  defects on the large object. These defects are defined by their lengths  $l_d^{(j)}$  and widths  $w_d^{(j)}$  and by the position of their lower left corners  $(x_d^{(j)}, y_d^{(j)})$  ( $j = 1, \dots, m$ ). In other words, due to some material deficiency, there are regions on the large object to which no small item is to be assigned. Every single region is contained in the smallest possible rectangle with



edges parallel to the edges of the large object. Figure 1 shows an example for such a defect with length  $l_d$ , width  $w_d$  and lower left corner  $(x_d, y_d)$ . In every feasible cutting pattern, no small item must overlap with this rectangle.



**Fig. 1:** Representation of a single defect on the large object

The above-given mathematical formulation remains valid for this problem variant, since the defects are only implicitly contained in the model via the postulation of a feasible cutting pattern.

### 3 Identification of Problem Parameters

In this section, the parameters of the Two-Dimensional Rectangular Single Large Object Placement Problem With Defects (2D\_R\_SLOPP\_DEF) will be identified, and it will be explained why they are a sensible choice for and how they will be included in the problem generator. These parameters (or, more precisely, a specific set of parameter values) are then used as descriptors for homogeneous problem classes.

Table 1 gives an overview of the parameters of the 2D\_R\_SLOPP\_DEF, which will be described in more detail in the following sections.

$n$	number of small item types
$m$	number of defects
$(L, W)$	dimensions of the large object
$s_l$	lower bound for the relative size of item types w.r.t. size of the large object
$s_u$	lower bound for the relative size of item types w.r.t. size of the large object
$(l_d^{(j)}, w_d^{(j)})$	dimensions of defect $j$ ( $j = 1, \dots, m$ )
$(x_d^{(j)}, y_d^{(j)})$	location of defect $j$ ( $j = 1, \dots, m$ )

**Table 1:** Problem parameters of the 2D\_R\_SLOPP\_DEF

### 3.1 Number of Small Item Types

The number  $n$  of small item types is a very straightforward candidate for a parameter of the 2D\_R\_SLOPP\_DEF, as it is a common measure for the problem size. It can be expected that the problem becomes more difficult to solve with a growing number of item types as the number of possible cutting patterns increases (for example, for only one item type, the optimal solution can be calculated applying a simple formula, at least if a guillotineable layout is assumed), yet it is expected that the solution quality also increases.

In the problem generator, this parameter is introduced as a controllable one, i.e. it can be fixed to an appropriate value by the user.

### 3.2 Dimensions of the Large Object

It has already been said in Section 2 that the problem data can be multiplied by a constant factor without changing the model. Hence, the absolute size of the large object is not too important, but its relative size in relation to the small item types and the defects. Yet, it can be assumed that the shape of the large object (quadratic, rectangular) is an influencing factor on how difficult it is to solve the problem, as a quadratic large object is probably easier to cut down than a very long and very narrow large object of the same area. As a consequence, we introduce the length and width of the large object as problem parameters.

Again, these parameters are controllable and can be explicitly defined by the user of the problem generator.

### 3.3 Relative Size of the Item Types

The sizes of the small item types are also likely to have an impact on the difficulty of the 2D\_R\_SLOPP\_DEF. We measure the size of an item type by its area which is given as  $a_i = l_i \cdot w_i$ . Small items allow for more and more sophisticated cutting patterns so that the solution quality is expected to increase, whereas the solution time is expected to drop.

The influencing factor is not the absolute, but the relative size of the item types in relation to the area of the large object. This relative size can be controlled by the user via the two descriptors  $s_l$  and  $s_u$ , which represent the lower and the upper bound for the relative size of the item types w.r.t. the area of the large object.

As it seems not reasonable – and not manageable – to keep control over every possible shape of the item types, the area of the item types is a sensible-chosen representative for the size. It will be described in more detail in Section 4 how the generation of “degenerated” item types (very long but very narrow) can be avoided.

### 3.4 Dimensions of the Defects

As we consider a cutting problem including material defects, at least one parameter has to be related to the set of defects. One candidate for this is their size. Unlike the small item types, length and width of the defects rather than their area are identified as an influencing factor and as a controllable parameter because, if there are only a few defects present, the shape of the defects can be assumed to have a strong

influence on how difficult a problem is to solve. Although having the same area, narrow defects which almost divide the large object in two or more objects and, thus, practically leaves us with two or more standard 2D\_R\_SLOPP, are expected to provide a very different challenge than big quadratic defects on the large object.

### 3.5 Locations of the Defects

The locations of the defects on the large object (represented by their lower left corners) are not included as controllable problem parameters, but are depicted as realizations of random variables. The reason for this is that their influence on the difficulty of the problem can be assumed to be strongly dependent on the size and shape of the large object and the defects and can thus not be defined independently in a sensible way.

## 4 Generation of Test Problem Instances

In the course of testing algorithms, a random sample of problem instances from a set of problem classes of the 2D\_R\_SLOPP\_DEF will have to be provided. Each problem class is defined by the set of parameters (or descriptors)  $(L, W, n, s_l, s_u, l_d^{(1)}, \dots, l_d^{(m)}, w_d^{(1)}, \dots, w_d^{(m)})$  specified above.

A specific problem class given through the values of  $L, W, n, s_l, s_u, l_d^{(j)}$  and  $w_d^{(j)}$  ( $j = 1, \dots, m$ ) forms the basis for problem instances which can be interpreted as a realization of a random variable  $(l_1, \dots, l_n, w_1, \dots, w_n, (x_d^{(1)}, y_d^{(1)}), \dots, (x_d^{(m)}, y_d^{(m)}))$ . For the generation of a problem instance, these values have to be fixed randomly. Section 4.2 deals with generating the dimensions of the item types, whereas in Section 4.3, the generation of the locations of the defects is considered in detail. Before that, a short description of the pseudo-random number generator used within this implementation is given.

### 4.1 Generation of Uniformly Distributed Pseudo-Random Numbers

Instead of using any built-in pseudo-random number generator (which may be dependent on the computer the program is running on), the problem generator includes an implementation, which ensures the portability of the generator as well as the reproducibility of the results. The implemented pseudo-random number generator is the one that has also been used by Gau and Wäscher (1995), and which is a special variant of the method attributed to Lehmer (Hutchinson (1966)). Only a very brief description shall be given here, similar to the one in Gau and Wäscher (1995).

Let a prime number  $p$  and an integer  $c \in \{1, \dots, p-1\}$  be given. After defining an integer number  $r_1 \in \{1, \dots, p-1\}$  as a “seed” (an initial number), a sequence of uniformly distributed integer random numbers is defined through the recursive formula

$$r_{n+1} = c \cdot (r_n \bmod p).$$

A sequence of uniformly distributed random numbers in the interval  $(0,1)$  can thus be obtained by dividing the integer random numbers by  $p$ .

An appropriate choice for  $p$  and  $c$  (Park and Miller (1988)) is

$$p = 2^{31} - 1 = 2,147,483,647 \quad \text{and} \quad c = 16,807.$$

Due to the size of the numbers, a direct calculation of the product of  $c$  and  $r_n$  is not possible on most contemporary computers. Yet, this problem can be solved by an approximate factorization of  $p$  in the following way:

Let

$$p = c \cdot q + t$$

where

$$q = p \operatorname{div} c \quad (\text{integer part of } p) \quad \text{and} \quad t = p \operatorname{mod} c.$$

With values for  $p$  and  $c$  as introduced above, we obtain

$$q = 127,773 \quad \text{and} \quad t = 2,836.$$

The desired value  $c \cdot r_n \operatorname{mod} p$  can now be calculated as follows (involving only numbers up to  $p$ ):

$$c \cdot r_n \operatorname{mod} p = \begin{cases} c \cdot (r_n \operatorname{mod} q) - t \cdot (r_n \operatorname{div} q) & \text{if } c \cdot (r_n \operatorname{mod} q) - t \cdot (r_n \operatorname{div} q) \geq 0 \\ c \cdot (r_n \operatorname{mod} q) - t \cdot (r_n \operatorname{div} q) + p & \text{otherwise.} \end{cases}$$

The seed  $r_1$  has not been chosen in advance. Thus, if this problem generator is used for testing algorithms, the seed used should always be published together with the results, due to reproducibility of the test data.

## 4.2 Determination of Item Type Dimensions

It has already been stated that all dimensions  $(l_i, w_i)$ ,  $i = 1, \dots, n$ , of the item types can be considered as integer values without loss of generality. The following procedure is used to determine the values: A realization  $\hat{a}_i$  (the preliminary area of item type  $i$ ) of a random variable  $A_i$  which is uniformly distributed in the interval  $[s_l \cdot LW, s_u \cdot LW]$  is generated. Note that this number is not required to be integer. To avoid the generation of biased items, which would occur if length and width would be generated directly, we generate the aspect ratio

$$b_i = \frac{l_i}{l_i + w_i} \tag{1}$$

and use this value to calculate  $l_i$  and  $w_i$ .

To guarantee non-biased problem instances, every item type generated fits on the large object. Therefore it is necessary to limit  $b_i$  to an interval chosen in a way that  $l_i$  will not exceed  $L$  and  $w_i$  will not exceed  $W$ . In detail, the following conditions hold if item type  $i$  fits on the large object:

$$l_i \cdot w_i = \hat{a}_i \tag{2}$$

$$l_i \leq L \tag{3}$$

$$w_i \leq W \Leftrightarrow \frac{\hat{a}_i}{l_i} \leq W \Leftrightarrow \frac{\hat{a}_i}{W} \leq l_i \tag{4}$$

(2) can be written as  $w_i = \frac{\hat{a}_i}{l_i}$ . Inserting this into (1) and solving for  $l_i$  gives

$$l_i = \sqrt{\frac{\hat{a}_i \cdot b_i}{1 - b_i}}. \quad (5)$$

Inserting this formula for  $l_i$  into (3) and (4) gives the following feasible interval for  $b_i$ :

$$\frac{\hat{a}_i}{\hat{a}_i + W^2} \leq b_i \leq \frac{L^2}{\hat{a}_i + L^2}. \quad (6)$$

Furthermore, it is desirable to avoid “degenerated” item types which are very long, but very narrow. Thus  $b_i$  is limited to the interval  $[0.1, 0.9]$ . If necessary and desired, the interval can be adjusted in the source code.

Summing up,  $b_i$  is generated as a realization of a random variable  $B_i$  which is uniformly distributed in the interval  $[b_l, b_u]$  where

$$b_l = \max \left\{ \frac{\hat{a}_i}{\hat{a}_i + W^2}, 0.1 \right\} \text{ and} \quad (7)$$

$$b_u = \min \left\{ \frac{L^2}{\hat{a}_i + L^2}, 0.9 \right\}. \quad (8)$$

Preliminary values for  $l_i$  and  $w_i$  are then calculated as follows:

$$\hat{l}_i = \sqrt{\frac{\hat{a}_i \cdot b_i}{1 - b_i}} \quad \text{and} \quad (9)$$

$$\hat{w}_i = \frac{\hat{a}_i}{\hat{l}_i}. \quad (10)$$

Both values are rounded to the nearest integer to obtain  $l_i$  and  $w_i$ , which gives an item type with an area  $a_i = l_i \cdot w_i$  which is very close to the randomly generated value  $\hat{a}_i$ .

Due to the rounding throughout the process, it may will happen that the area  $a_i$  does not lie within the feasible interval  $[s_l \cdot LW, s_u \cdot LW]$ . If this is the case, the following adjustment procedure is applied. Assuming that  $a_i$  is too small, item type  $i$  is then adapted in the following way (an analogous procedure is used if  $a_i$  is too large): A realization  $k$  of a random variable  $K$  which is uniformly distributed in the interval  $[0, 1]$  is generated. If  $k < 0.5$  and if it is feasible,  $l_i$  is augmented by 1. (The augmentation of  $l_i$  is feasible if  $l_i < L$ ,  $(l_i + 1) \cdot w_i \leq s_u \cdot LW$  and  $\frac{l_i + 1}{(l_i + 1) + w_i} \leq 0.9$ .) Otherwise  $w_i$  is augmented by 1, if feasible. The area  $a_i$  is recalculated, and it is checked if it lies within the feasible interval now. If this is not the case, the adjustment procedure starts again.

(Note that there are some restrictions for an augmentation of  $l_i$  or  $w_i$ . It is even possible that there is no feasible augmentation. In that case it is not possible to find values for  $l_i$  and  $w_i$  that meet the restrictions. This case can be avoided by choosing  $s_l, s_u, L$  and  $W$  in such a way that  $LW \cdot (s_u - s_l)$  is sufficient large.)

### 4.3 Determination of the Locations of the Defects

Let  $(x_d, y_d)$  be the lower left corner of a defect with length  $l_d$  and width  $w_d$ . Then the position of the lower left corner,  $(x_d, y_d)$ , has to fulfill the following properties:  $x_d$  must lie within the interval  $[0, L - l_d]$  and  $y_d$  must lie within the interval  $[0, W - w_d]$ . Thus, realizations  $\hat{x}_d$  of a random variable  $X$ , which is uniformly distributed in the interval  $[0, L - l_d]$ , and  $\hat{y}_d$  of a random variable  $Y$ , which is uniformly distributed in the interval  $[0, W - w_d]$  are generated. These values are then rounded mathematically to obtain  $x_d$  and  $y_d$ .

Yet, each defect has to be treated as an individual, single defect for the particular set of item types it is generated for, as it is not checked if the defects overlap.

### 4.4 Implementation

The problem generator described in this section has been coded in C and compiled with the free compiler Bloodshed Dev-C++ (in order to enable everyone interested to recompile the code with adapted specifications). The problem parameters can be entered via a dialog window when running the program.

A version executable under Windows as well as the source code of the problem generator are available at [www.mansci.ovgu.de/mansci/en/research/materials](http://www.mansci.ovgu.de/mansci/en/research/materials).

## 5 Numerical Example

In order to demonstrate the functioning of the problem generator, a few examples of instances from a specific problem class will be shown in this section.

The pseudo-random number generator has been initialized by using the value 123456 as a seed. For the examples presented in this section, the parameters of the problem have been chosen as given in Table 2.

number of instances	50
dimensions of the large object	(400,300)
number of item types	10
lower bound for relative size of item types	0.01
upper bound for relative size of item types	0.05
number of defects per instance	3
dimensions of the 1st defect	(5,5)
dimensions of the 2nd defect	(10,15)
dimensions of the 3rd defect	(40,20)

**Table 2:** Parameter choices for the example

From the 50 problem instances provided by the problem generator, the first and the last one are given in Table 3.

Instance 01				Instance 50			
item types				item types			
i	length	width	area	i	length	width	area
1	15	122	1830	1	40	87	3480
2	31	57	1767	2	43	92	3956
3	172	30	5160	3	94	46	4324
4	46	122	5612	4	72	57	4104
5	72	47	3384	5	208	24	4992
6	51	30	1530	6	19	138	2622
7	23	79	1817	7	50	48	2400
8	58	76	4408	8	15	118	1770
9	143	21	3003	9	16	94	1504
10	21	75	1575	10	53	77	4081
defects				defects			
no.	lower left corner	upper right corner		no.	lower left corner	upper right corner	
1	232	102	237 107	1	289	242	294 247
2	58	243	68 258	2	364	49	374 64
3	191	11	231 31	3	190	204	230 224

**Table 3:** Selected problem instances of the numerical example

## 6 Remarks

The problem generator described in this paper has been developed in order to be able to test algorithms for the 2D\_R\_SLOPP\_DEF. By ignoring the data of the defects, the problem instances can also be applied to testing algorithms for the 2D\_R\_SLOPP without any defect. Apart from that, it is also directly applicable for both the 2D\_R\_SLOPP\_DEF and the 2D\_R\_SLOPP if the rotation constraint is imposed and / or if a guillotineable cutting pattern layout is required.

The problem instances generated are suitable for unweighted problems (the value of each item type equals its area). Only minor modifications in the code are necessary to enable the problem generator to provide a specific value for each item type and, thus, instances for weighted problems.



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